

# AP Calculus

Chapter 1

Section 1-2

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## Functions

A **function** from a set  $D$  to a set  $R$  is a rule that assigns a unique element in  $R$  to each element in  $D$ .

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### Functions

$f(x) = x^2$

$y = x^2$

$x$	$y$
-2	4
-1	1
0	0
1	1
2	4

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### Functions

$A = \pi r^2$

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## Function Domain

$$f(x) = \frac{x^2 + 4x - 32}{x - 4} \rightarrow \frac{(x+8)(\cancel{x-4})}{\cancel{x-4}}$$

$$x - 4 \neq 0 \rightarrow x \neq 4$$

$$x < 4 \cup x > 4$$

$$(-\infty, 4) \cup (4, \infty)$$

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## Function Domain

$$f(x) = \frac{x + 3}{\sqrt{4 - x^2}}$$

$$4 - x^2 \geq 0$$

$$4 - x^2 \neq 0$$

$$4 - x^2 > 0$$

$$4 > x^2$$

$$-2 < x < 2$$

$$(-2, 2)$$

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## Even and Odd Functions

A function  $y = f(x)$  is an

**even function** of  $x$  if  $f(-x) = f(x)$ ,

**odd function** of  $x$  if  $f(-x) = -f(x)$ ,

for every  $x$  in the function's domain.

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## Even, Odd, or Neither

$$f(x) = x^4$$

$$f(-x) = (-x)^4 = x^4$$

even

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## Even, Odd, or Neither

$$f(x) = x^4 + 1$$

$$f(-x) = (-x)^4 + 1$$
$$x^4 + 1$$

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## Even, Odd, or Neither

$$f(x) = (x + 1)^4$$

$$f(-x) = (-x + 1)^4$$

neither

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## Even, Odd, or Neither

$$f(x) = x^3 + 1$$

$$f(-x) = -x^3 + 1$$

neither

$$f(x) = (x - 2)^3$$

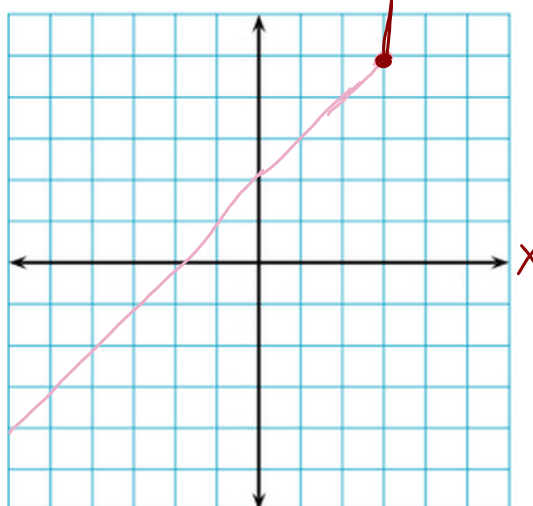
$$f(-x) = (-x - 2)^3$$

neither

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## Piecewise Functions

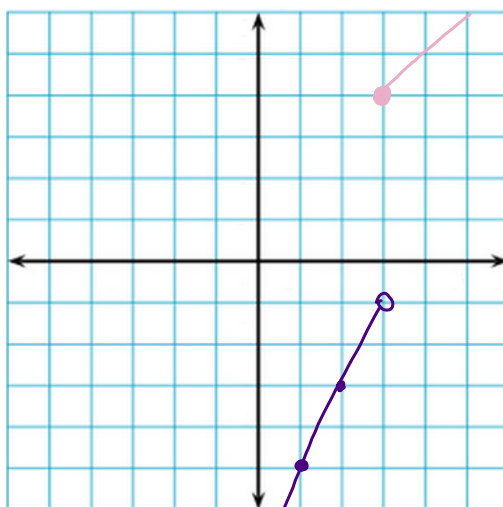
$$f(x) = \begin{cases} x + 2, & x < 3 \\ x^2 - 4, & x \geq 3 \end{cases}$$



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## Piecewise Functions

$$f(x) = \begin{cases} 2x - 7, & x < 3 \\ x + 1, & x \geq 3 \end{cases}$$



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## Composition of Functions

$$f(x) = 7x^3 - x$$

$$g(x) = x^{-1}$$

$$f \circ g(x) = 7(x^{-1})^3 - (x^{-1}) = 7x^{-3} - x^{-1}$$

$\leftarrow$   
 $f(g(x))$

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## Composition of Functions

$$f(x) = 7x^3 - x$$

$$g(x) = x^{-1}$$

$$g \circ f(x) = (7x^3 - x)^{-1}$$

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The radius of the great circle of a spherical balloon is growing at a constant rate of 1.5 feet per minute for  $0 \leq t \leq 18$ . Write a function,  $r(t)$ , to describe the growth of the radius. Then write a function  $A(t)$  to describe the growth of the area of the great circle.

$$r(t) = 1.5t \quad A(r) = \pi r^2$$

$$A(r(t)) = \pi (1.5t)^2 \text{ ft}^2$$

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# Homework

Pages 19 - 20

Do odd #s: 1 - 11, 21 - 33, 41 - 47, 51 - 55

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