

Warm-up

Find the instantaneous rate of change (the derivative) for the functions...

$$y = 2x^2 + 1 \text{ at } x = a$$

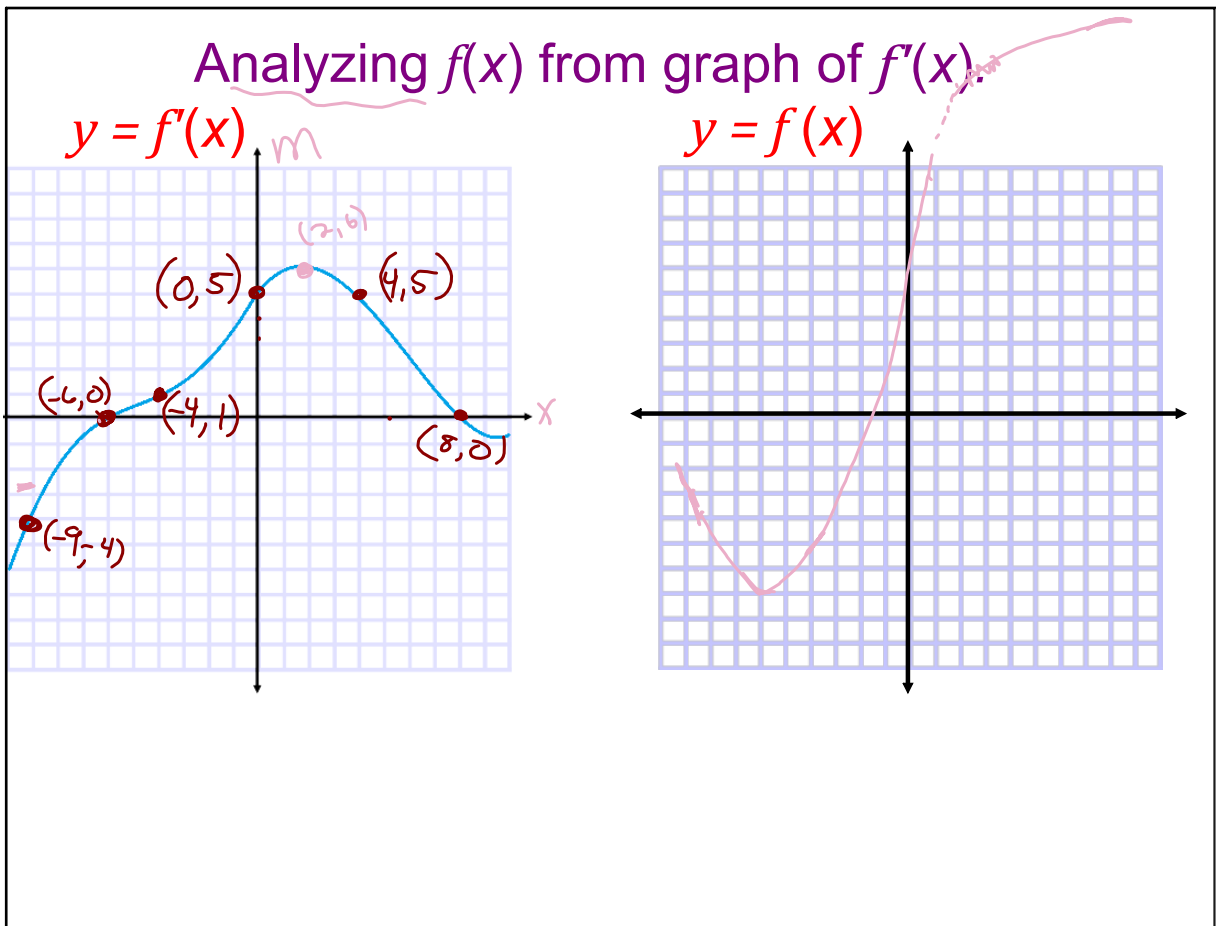
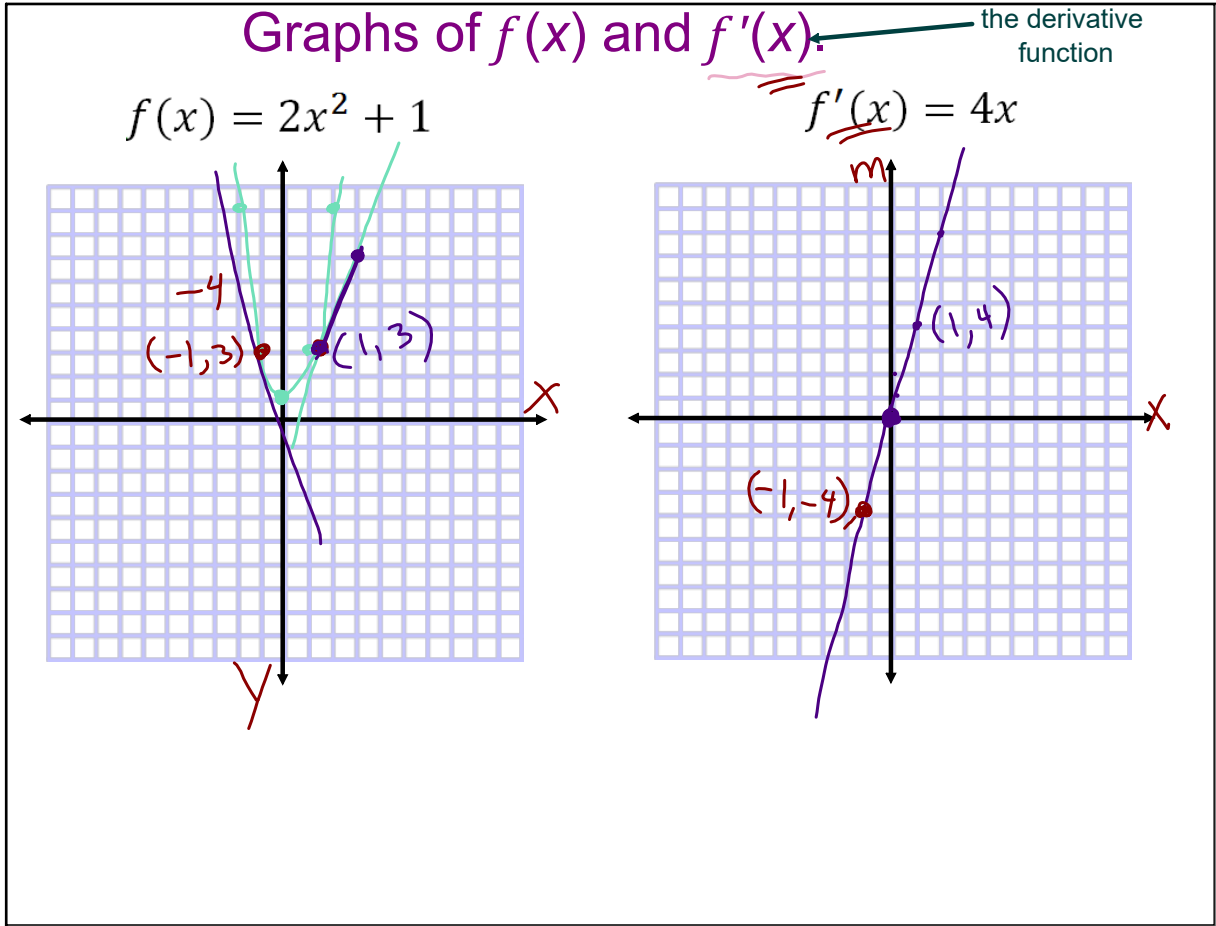
$$y = 2x^2 + 10 \text{ at } x = a$$

Dec 4-10:44 AM

Calc 4 Life

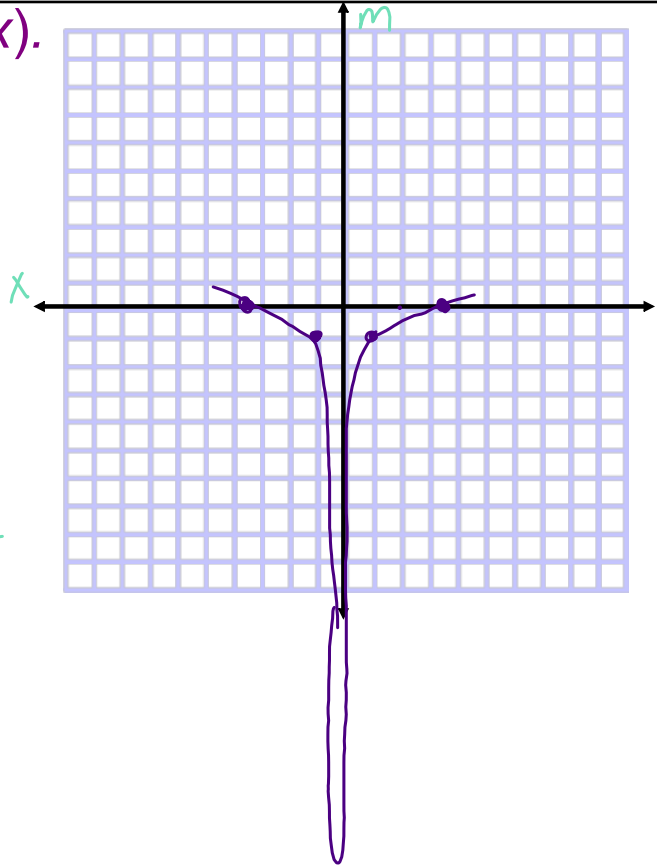
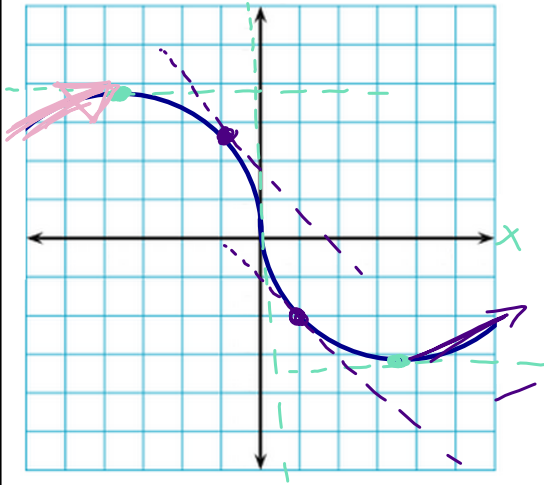
Section 3.5

May 13-10:02 PM



Graphing $f'(x)$ from $f(x)$.

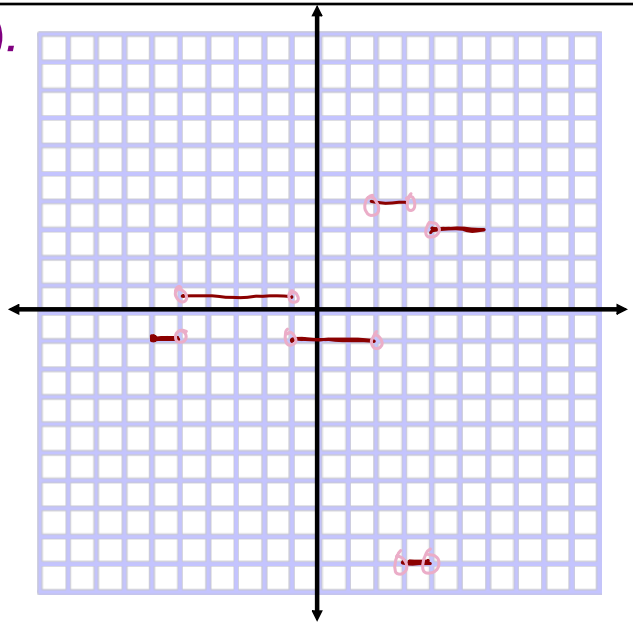
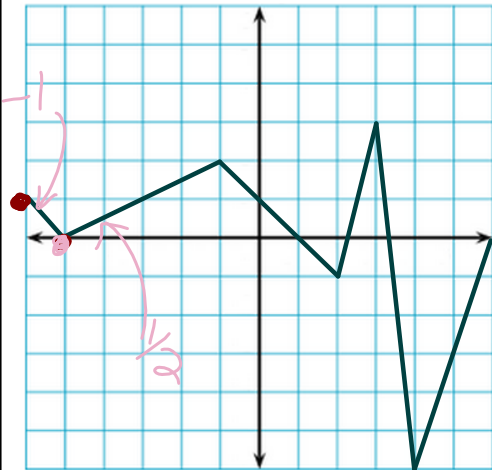
$y = f(x)$



Sep 25-8:11 AM

Graphing $f'(x)$ from $f(x)$.

$y = f(x)$



Sep 25-8:11 AM

Warm-up Day 2

Find the instantaneous rate of change (the derivative) for the function $f(x) = \frac{1+x^2}{x}$ at $x = x$.

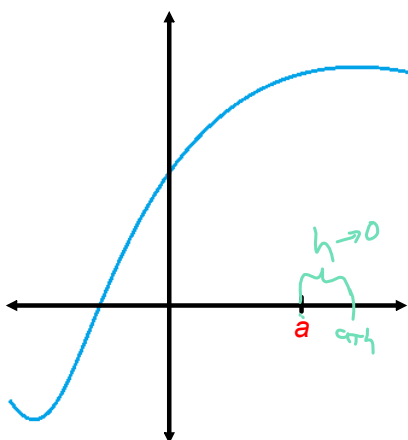
Then use a graphing utility to sketch a graph of the function $y = f(x)$ and its derivative, $f'(x)$.

Dec 4-10:44 AM

Definitions of Derivative

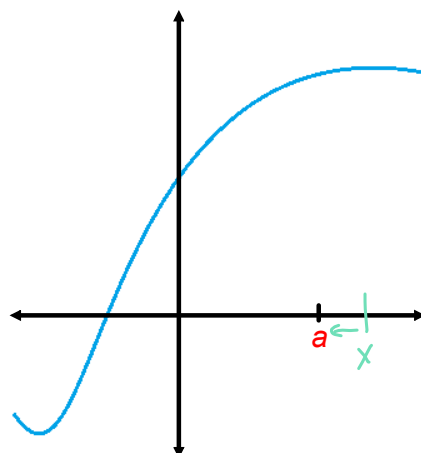
Definition

$$\lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{(a+h) - a}$$



Alternate Definition

$$\lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$



Sep 25-8:15 AM

Find the derivative for the functions using the alternate definition...

$y = 2x^2 + 1$ at $x = 4$
 $2(4)^2 + 1 = 33 \stackrel{a=4}{=} f(4)$

$$\lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a} = \frac{2x^2 + 1 - 33}{x - 4} = \frac{2(x^2 - 16)}{x - 4} = \frac{2(x+4)(x-4)}{x-4}$$

$y = x^6 + x$ at $x = a$
 $\stackrel{a}{=} (a^6 + a)$

$$\lim_{x \rightarrow a} \frac{x^6 + x - a^6 - a}{x - a} = \frac{(x^6 - a^6) + (x - a)}{x - a}$$

$$= \frac{(x^3 - a^3)(x^3 + a^3) + (x - a)}{x - a}$$

$$\lim_{x \rightarrow a} \frac{\cancel{(x-a)}(x^2 + ax + a^2)(x^3 + a^3) + \cancel{(x-a)}}{\cancel{x-a}}$$

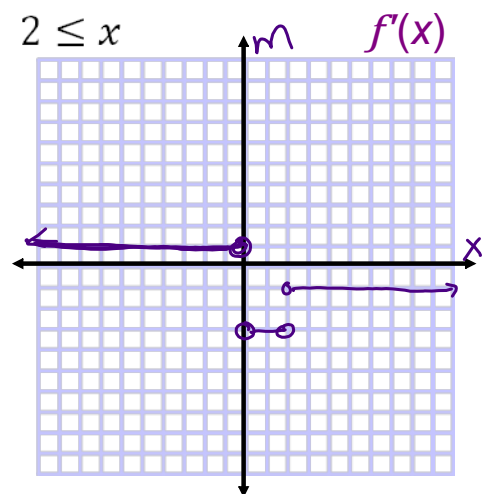
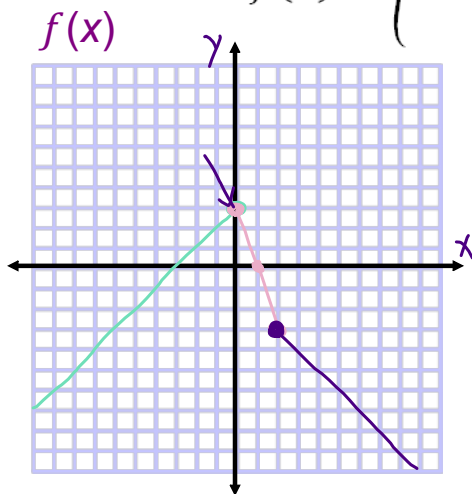
$$= \frac{(a^2 + a^2 + a^2)(a^3 + a^3) + 1}{(3a^2)(2a^3) + 1} = 6a^5 + 1$$

Dec 4-10:44 AM

One-Sided Derivatives

Graph $f(x)$ and $f'(x)$.

$$f(x) = \begin{cases} x + 3, & x < 0 \\ -3x + 3, & 0 \leq x < 2 \\ -x - 1, & 2 \leq x \end{cases}$$

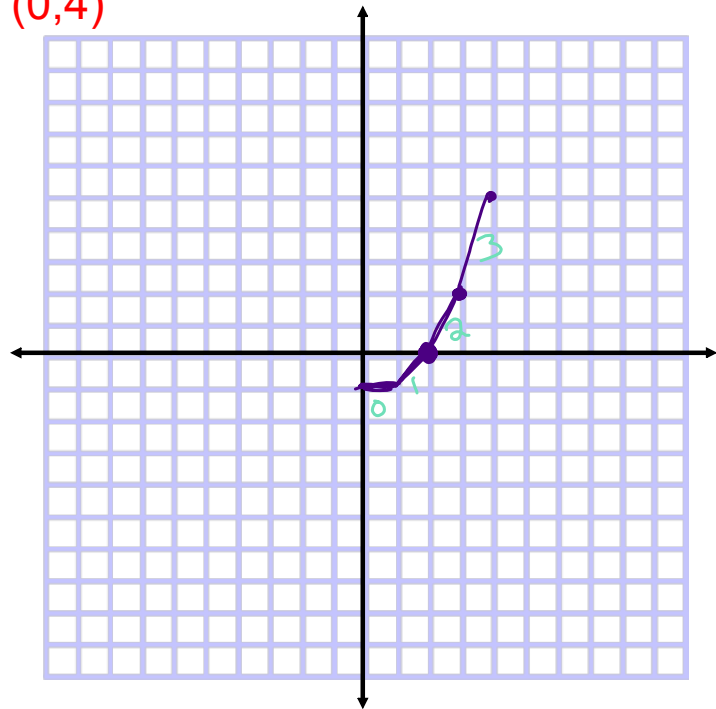
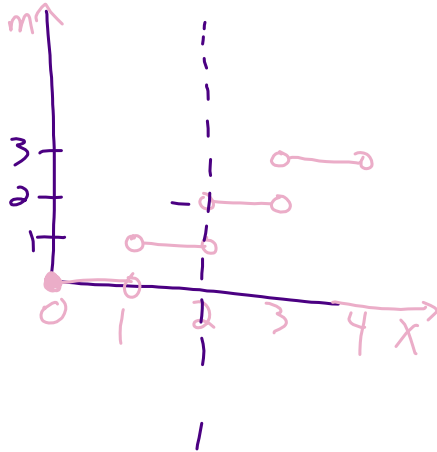


Sep 26-8:53 AM

Sketching $f(x)$ from $f'(x)$.

Sketch a graph with the following characteristics:

- $f'(x) = \text{int } x$, $0 < x < 4$ and $x \neq 1, 2, \text{ or } 3$
- $f(x)$ is continuous on $(0,4)$
- $f(2) = 0$



Sep 25-8:11 AM

Homework

Page 189 - 190

9-14 all, 17, 25

Page 181

21b - 26b (only part b, using alternate definition)

May 13-10:02 PM